

Directions: *Work on these sheets.*

**Part 1: Multiple Choice.** *Circle the letter corresponding to the best answer.*

- Which of the following pairs of events are disjoint (mutually exclusive)?
  - A: the odd numbers; B: the number 5
  - A: the even numbers; B: the numbers greater than 10
  - A: the numbers less than 5; B: all negative numbers
  - A: the numbers above 100; B: the numbers less than -200
  - A: negative numbers; B: odd numbers
- Which of the following are true?
  - The sum of the probabilities in a probability distribution can be any number between 0 and 1.
  - The probability of the union of two events is the sum of the probabilities of those events.
  - The probability that an event happens is equal to  $1 -$  (the probability that the event does not happen).
  - I and II only
  - I and III only
  - II and III only
  - I, II, and III
  - None of the above gives the complete set of true responses
- Government data show that 26% of the civilian labor force has at least 4 years of college and that 15% of the labor force works as laborers or operators of machines or vehicles. Can you conclude that because  $(0.26)(0.15) = .039$  about 4% of the labor force are college-educated laborers or operators?
  - Yes, by the multiplication rule
  - Yes, by conditional probabilities
  - Yes, by the law of large numbers
  - No, because the events are not independent
  - No, because the events are not mutually exclusive
- If a peanut M&M is chosen at random, the chances of it being of a particular color are shown in the table below.

<u>Color</u>	<u>Brown</u>	<u>Red</u>	<u>Yellow</u>	<u>Green</u>	<u>Orange</u>	<u>Blue</u>
Probability	.3	.2	.2	.2	.1	

The probability of randomly drawing a blue peanut M&M is

- 0.1
- 0.2
- 0.3
- 1.0
- According to this distribution, it's impossible to draw a blue peanut M&M.

5. If  $A \cup B = S$  (sample space),  $P(A \text{ and } B^c) = 0.25$ , and  $P(A^c) = 0.35$ , then  $P(B) =$
- (a) 0.35
  - (b) 0.4
  - (c) 0.65
  - (d) 0.75
  - (e) None of the above. The answer is \_\_\_\_\_.

**Part 2: Free Response**

*Answer completely, but be concise. Write sequentially and show all steps.*

A box contains six red tags numbered 1 through 6, and four white tags numbered 1 through 4. One tag is drawn at random.

6. Write the sample space for this experiment.

Calculate the following probabilities:

- |                                      |                                      |
|--------------------------------------|--------------------------------------|
| 7. $P(\text{red})$                   | 8. $P(\text{even number})$           |
| 9. $P(\text{red and even})$          | 10. $P(\text{red or even})$          |
| 11. $P(\text{neither red nor even})$ | 12. $P(\text{even} \mid \text{red})$ |
| 13. $P(\text{red} \mid \text{even})$ | 14. $P(<4 \mid \text{odd})$          |
15. Suppose that for a group of consumers, the probability of eating pretzels is .75 and that the probability of drinking Coke is .65. Further suppose that the probability of eating pretzels *and* drinking Coke is .55. Determine if these two events are *independent*.

Consider the following experiment: The letters in the word AARDVARK are printed on square pieces of tagboard (same size squares) with one letter per card. The eight letter cards are then placed in a hat, and one letter card is randomly chosen (without looking) from the hat.

16. List the sample space  $S$  of all possible outcomes.

$$S = \{$$

17. Make a table that shows the set of outcomes ( $X$ ) and the probability of each outcome:

<u>Outcomes</u>
$P(X)$

18. Consider the following events:

V: the letter chosen is a vowel.

F: the letter chosen falls in the first half of the alphabet (i.e., between A and M).

List the outcomes in each of the following events, and determine their probabilities:

$$V = \{ \qquad \qquad \qquad P(V) =$$

$$F = \{ \qquad \qquad \qquad P(F) =$$

$$V \text{ or } F = \{ \qquad \qquad \qquad P(V \text{ or } F) =$$

$$\text{complement of } F = \{ \qquad \qquad \qquad P(F^c) =$$

19. Determine if the events  $V$  and  $F$  are independent.

Here is the assignment of probabilities that describes the age (in years) and the sex of a randomly selected American student.

Age	14-17	18-24	25-34	$\geq 35$
Male	.01	.30	.12	.04
Female	.01	.30	.13	.09

20. What is the probability that the student is a female?
21. What is the conditional probability that the student is a female given that the student is at least 35 years old?
22. What is the probability that the student is either a female or at least 35 years old?
23. If four cards are drawn from a standard deck of 52 playing cards and not replaced, find the probability of getting at least one heart.
24. If three dice are rolled, find the probability of getting triples – i.e., 1,1,1 or 2,2,2 or 3,3,3 etc.

*I pledge that I have neither given nor received aid on this test:* \_\_\_\_\_